

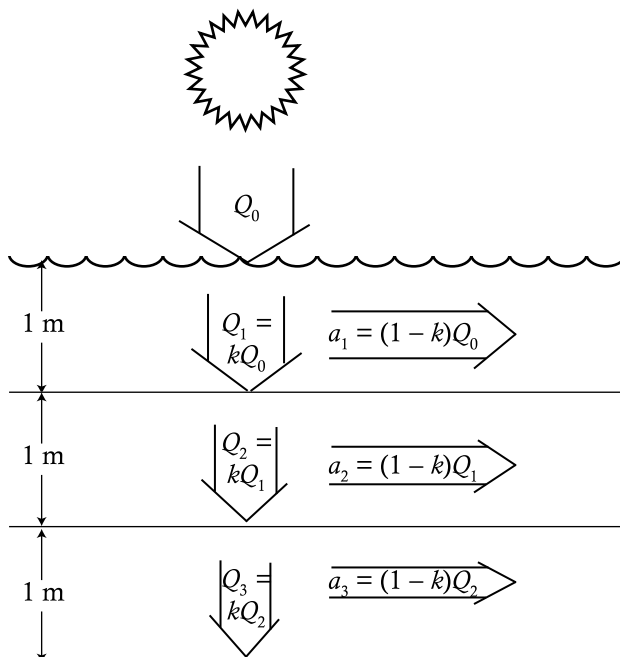
## Exercise 2

A model of how deeply solar radiation penetrates into an ocean or lake can be made by assuming a certain transmission fraction ( $k$ ) passes through each meter of depth. Thus, if  $Q_0$  is the amount of insolation entering the top of the water column, then  $Q_1 = kQ_0$  is how much there is left at one meter down,  $Q_2 = kQ_1 = k^2Q_0$  is how much there is left at two meters down, and so on:  $Q_j = kQ_{j-1} = \dots = k^jQ_0$ . To program this for a model, where  $Q_0$  is known, we use the recursive part of the equation:

$$Q_j = k \times Q_{j-1}$$

The energy that is *not* transmitted through each layer is absorbed in that layer to warm it up. (That is conservation of energy in simple form: the solar radiation must be either absorbed into heat or passed along.) So the energy absorbed into the first one-meter-thick layer is  $a_1 = (1 - k)Q_0$ , the energy absorbed in the second layer is  $a_2 = (1 - k)Q_1 = (1 - k)kQ_0$ , and in general:

$$a_j = (1 - k) \times Q_{j-1}$$



Write a program that prints a table to the screen of transmitted ( $Q$ ) and absorbed ( $a$ ) radiation at each of the first 20 one-meter-thick layers of the ocean. To simplify this, you may set the starting point at an incident  $Q_0 = 100$  so that results are expressed as a percentage of net surface (bottom-of-atmosphere) downwelling shortwave radiation. The value of  $k$  varies with sun angle and turbidity of the water, so you should start by asking the user to input a value of  $k$  and reading that value from the keyboard.

To assist in debugging your program, the value of  $a$  in the 20th layer will be 0.034, 0.288, and 1.351 for values of  $k = 0.7, 0.8,$  and  $0.9,$  respectively. Solving this problem without a `DO` loop (such as by using the editor to copy some lines of code many times and edit them) is *not acceptable*. You will be working on this table before we get to formatting output, so you may use default formatting and have uneven columns for this exercise. (10 points)

**For further thought:** This model does not include backscattering, in which some shortwave radiation enters each layer by scattering from below. There should be an additional reflection parameter,  $r$ , which takes some fraction of the  $kQ_{j-1}$  and sends it back to layer  $j - 1$ . That is a small effect for an ocean, and was left out to make this program simple enough for a first programming exercise.